## Quantum behaviour Answers to practice questions

| Question | Answer | Marks |
| :---: | :---: | :---: |
| 1 | A | 1 |
| 2 | Energy of a photon of light of wavelength 400 nm $\begin{aligned} & =\frac{6.6 \times 10^{-34} \mathrm{~J} \mathrm{~s} \times 3 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1}}{400 \times 10^{9} \mathrm{~m}} \\ & =4.95 \times 10^{-19} \mathrm{~J} \end{aligned}$ <br> Number of photons emitted per second $=$ energy emitted per second/energy per photon $=18 \times 10^{-3} \mathrm{~J} / 4.95 \times 10^{-19} \mathrm{~J}(1)=3.6 \times 10^{16}$ photons. <br> Number of photons emitted per second = energy emitted per second/energy per photon $\begin{aligned} & =\frac{18 \times 10^{-3} \mathrm{~J}}{4.95 \times 10^{-19} \mathrm{~J}} \\ & =3.6 \times 10^{16} \text { photons } \end{aligned}$ | 1 <br> 1 <br> 1 <br> 1 1 |
| 3 | $\begin{aligned} & \text { Momentum of electron }=\sqrt{2 m E_{\mathrm{k}}} \\ & =\left(2 \times 9.11 \times 10^{-31} \mathrm{~kg}^{2} 1.6 \times 10^{3} \mathrm{eV} \times 1.6 \times 10^{-19} \mathrm{C}\right)^{\frac{1}{2}} \\ & =2.159 \ldots \times 10^{-23} \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1} \\ & \text { De Broglie wavelength }=\frac{6.6 \times 10^{-34} \mathrm{~J} \mathrm{~s}}{2.159 . . \times 10^{-23} \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}} \\ & =3.11 \times 10^{-11} \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |
| 4 | $\begin{aligned} & \text { Energy required to release electron in } \mathrm{J}=3.7 \times 1.6 \times 10^{-19} \mathrm{~J} \\ & \text { k.e. } \text { max }=\frac{6.6 \times 10^{-34} \mathrm{~J} \mathrm{~s} \times 3 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1}}{170 \times 10^{-9} \mathrm{~m}}-3.7 \times 1.6 \times 10^{-19} \mathrm{~J} \\ & =5.7 \times 10^{-19} \mathrm{~J} \end{aligned}$ | $\begin{aligned} & 1 \\ & \\ & 1 \\ & 1 \end{aligned}$ |
| 5 | $\begin{aligned} & \text { Momentum of electron }=\frac{6.6 \times 10^{-34} \mathrm{~J} \mathrm{~s}}{6.6 \times 10^{-10} \mathrm{~m}}=1.0 \times 10^{-24} \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1} \\ & \begin{aligned} \text { Velocity of electron } & =\frac{1.0 \times 10^{-24} \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}}{9.11 \times 10^{-31} \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}} \\ & =1.1 \times 10^{6} \mathrm{~m} \mathrm{~s}^{-1} \end{aligned} \end{aligned}$ | 1 <br> 1 <br> 1 |
| 6 a | Phase difference of $2 \pi$ radians corresponds to one wavelength path difference, therefore, a path difference of $\frac{\lambda}{3}$ will correspond to a phase difference of $\frac{2 \pi}{3}$. | 1 |
| 6 b | Resultant forms an equilateral triangle. Length of resultant $=$ length of each individual phasor arrow | $\begin{aligned} & 1 \\ & 1 \\ & \hline \end{aligned}$ |
| 6 c | Length of resultant arrow at $P_{2}=2 \times$ length of individual phasor arrow. Ratio of lengths $=2$ | $\begin{array}{\|l\|} \hline 1 \\ 1 \\ \hline \end{array}$ |
| 6 d | $\begin{aligned} \text { Ratio } & =\frac{1^{2}}{2^{2}} \\ & =0.25 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |
| 6 e | Three phasors form equilateral triangle. <br> No resultant phasor. <br> This model gives a zero probability for a photon arriving at $\mathrm{P}_{1}$ when the three slits are open. | $\begin{aligned} & \hline 1 \\ & 1 \\ & 1 \\ & \hline \end{aligned}$ |

## 7 Quantum behaviour <br> Answers to practice questions

| 7 a | When the intensity of the light incident on the surface is doubled the number of electrons released per second will also double; as twice as many photons are striking the surface each second. As the energy of each individual photon is unchanged, the ejected photoelectrons will have the same maximum kinetic energy. | 1 1 1 1 |
| :---: | :---: | :---: |
| 7 b | $\begin{aligned} & 0.2 \mathrm{eV}=4.5 \times 10^{14} \mathrm{~Hz} \times h-\Phi \\ & 1.4 \mathrm{eV}=7.5 \times 10^{14} \mathrm{~Hz} \times h-\Phi \\ & 4.5 \times 10^{14} \mathrm{~Hz} \times h-0.2 \mathrm{eV}=7.5 \times 10^{14} \mathrm{~Hz} \times h-1.2 \mathrm{eV} \\ & 3.0 \times 10^{14} \mathrm{~Hz} \times h=1.2 \times 1.6 \times 10^{-19} \mathrm{~J} \\ & h=6.4 \times 10^{-34} \mathrm{~J} \mathrm{~s} \end{aligned}$ | 1 1 1 1 |
| 7 c | Using calculated value for $h$ : <br> Work function $=2.56 \times 10^{-19} \mathrm{~J}$ <br> Frequency $=\frac{2.56 \times 10^{-19} \mathrm{~J}}{6.4 \times 10^{-34} \mathrm{~J} \mathrm{~s}}=4.0 \times 10^{14} \mathrm{~Hz}$ <br> (Using $6.6 \times 10^{-34}$ gives the same value to 2 s.f.) | 1 1 |
| 8 a i | All in phase | 1 |
| 8 a ii | 3 A | 1 |
| 8 b i | One phasor rotation corresponds to $\lambda$. $120^{\circ}=1 / 3$ rotation for extra $\frac{\lambda}{3}$ | $1$ $1$ |
| 8 b ii | (Arrows correctly drawn in circles; three arrows add tip-to-tail to give zero resultant. | 1 |
| 8 b iii | $\sin \theta=\frac{\Delta x}{b / 3 \times 1}=\frac{\lambda / 3}{b / 3}=\frac{\lambda}{b} \operatorname{so~} \lambda=b \sin \theta$ | 1 |
| 8 c | $\begin{aligned} & \sin \theta=\frac{\lambda}{b}=\frac{2.4 \mathrm{~cm}}{6.0 \mathrm{~cm}}=0.40 \\ & \theta=24^{\circ}(2 \mathrm{~s} . \text { f. }) \end{aligned}$ | 1 1 |

