Oxford A Level Sciences

OCR Physics **B**

15 The Boltzmann factor Answers to practice questions

Question	Answer	Marks
1	В	1
2	С	1
3 a	kT represents an approximation for the mean particle energy.	1
3 b	<i>E</i> is much larger than kT at room temperature, giving a low chance of particles escaping the surface of the solid aluminium.	1
4 a	$E_{\rm k} \approx kT = 1.4 \times 10^{-23} \times 10000$ = 1.4 × 10 ⁻¹⁹ ~ 1.6 × 10 ⁻¹⁹ I	1
4 b	(Real gases are not ideal therefore) particles collide and energy is	1
	So particles will possess a range of energies.	1
5 a	$N_2 = e^{-\Delta E/kT}$ where $\Delta E = E_2 - E_1$	1
	<u>-1.6×10⁻¹⁸</u>	
	$N_2 = N_{\rm e}^{1.4 \times 10^{-23} \times 6000} = 5 \times 10^{-9} N$	1
5 b	The energy difference between E_3 and E_2 is different to the energy level between E_2 and E_1 .	1
	The equation $\frac{N_3}{N_2} = \frac{N_2}{N_1}$ would only work if the difference between energy	1
	levels were the same.	
6 a I	Energy required to evaporate 1 molecule =	
	$\frac{\text{energy required to evaporate r kg}}{\text{number of molecularity}} = \frac{E}{\text{mass}}$	
	$\frac{11233}{1123} \times N_{A}$	
	8.4×10 ⁵	
	$=\frac{0.4\times10}{1000}$	1
	$\frac{1000}{46} \times 6.02 \times 10^{23}$	
	$= 6.4 \times 10^{-20}$ J (1 s.f.)	1
6 a ii	$E \approx kT = 1.4 \times 10^{-23} \times 310$	1
	$= 4.34 \times 10^{-21} \text{ J}$	1
6 a iii	$e^{-\Delta E/\kappa T}$	1
	$-\frac{6.4 \times 10^{-20} \times 310}{1.4 \times 10^{-23}}$	1
	$= 0^{-1.4\times10}$ = 2.04 × 10 ⁻⁷ = 2 × 10 ⁻⁷	1
6 b	The proportion of ethanol molecules with enough energy to evaporate is	1
	greater than for water.	
	Therefore ethanol will evaporate from the skin faster than water	1
	and carry away energy at a higher rate.	1
7 a	$E \approx kT \times 1.4 \times 10^{-23} \times 300 = 4.2 \times 20^{-21} \text{ J}$	1
7 b	Potential energy = $mgh = 4.6 \times 10^{-26} \times 3000 \times 9.8 = 1.4 \times 10^{-21} \text{ J}$	1
7 c	<u>1.4×10⁻²¹</u>	
	Boltzmann factor = $e^{-E/kT}$ = $e^{1.4 \times 10^{-23} \times 300}$	
		1
7 d i	Boltzmann factor = $e^{-ingrav}$	1
	As it increases above sea level, the probability, according to the Boltzmann probability, that a particle will have the potential energy above	
	ground level energy to occupy that height decreases.	

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7 d ii	Any sensible suggestion, e.g.:	
	Calculate the ratio of density for a number of equally-spaced	1
	height intervals above sea level.	
	 If the ratio in each case is roughly the same then 	1
	The decrease is exponential.	1
7 e	The Boltzmann factor is given by $e^{-E/kT}$. As <i>T</i> increases, the value of $\frac{E}{kT}$	1
	decreases	1
	and so the value of the Boltzmann factor increases.	1
8 a	As gas molecules collide with the walls of a container they change	1
	velocity.	
	There is a corresponding change in momentum that requires an impulse or	1
	force.	
	I his force acting over an area of the container results in pressure within	1
	the container.	
8 b	$E \approx kI = 1.4 \times 10^{-3} \times 288$	1
	$= 4.032 \times 10^{-7} \text{ J} = 4 \times 10^{-7} \text{ J} (1 \text{ s.f.})$	1
8 C	$-\frac{3.4 \times 10^{-20}}{22}$	
	$e^{-E/kT} = e^{1.4 \times 10^{-23} \times 288}$	1
	$=2.17 \times 10^{-4}$	1
8 d i	As T increases, the Boltzmann factor increases exponentially.	1
8 d ii	Boltzmannfactor (360K) 12.5	
	Factor of increase = $\frac{1}{Roltzmannfactor(200K)} = \frac{12.0}{2.5}$	1
	6 = 0	1